

## Hydrothermal Preparation and Crystal Structure of $\text{NaHo}_4(\text{GeO}_4)_2\text{O}_2\text{OH}$

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The compound  $\text{NaHo}_4(\text{GeO}_4)_2\text{O}_2\text{OH}$  was prepared using hydrothermal techniques. The crystal structure was investigated using Patterson and Fourier functions and was refined to a conventional  $R$  value of 8.5 %. The space group is  $Pnma$  with  $a=6.75$  Å,  $b=21.67$  Å, and  $c=6.91$  Å. The holmium atoms are seven coordinated with oxygen atoms.

A hydrothermal investigation of the system  $\text{Ho}_2\text{O}_3-\text{H}_2\text{O}-\text{Na}_2\text{O}$  yielded the monoclinic form of holmium oxide hydroxide and single crystals of a phase of unknown composition in one experiment, where the system was contaminated with a small quantity of germanium dioxide. A three-dimensional X-ray analysis proved that this new phase had the formula  $\text{NaHo}_4(\text{GeO}_4)_2\text{O}_2\text{OH}$ .

### EXPERIMENTAL

*Chemistry.* Holmium trihydroxide was precipitated with a 2 M  $\text{NH}_3$  solution from a dilute solution of holmium nitrate, prepared by dissolving the oxide in nitric acid. The precipitated trihydroxide was washed with water, and was treated with a 1.5 M  $\text{NaOH}$  solution at 490°C, 1200 atm for 60 h in a pressure bomb lined with pure silver. The product was washed with water and dried in air at room temperature. The silver ampoule had previously been used in hydrothermal preparation of germanates.

*X-Ray technique.* A flat crystal with dimensions 0.0175 cm  $\times$  0.0063 cm  $\times$  0.0023 cm was investigated using Weissenberg and precession methods. Photographs were taken of  $(0kl)$ ,  $(1kl)$ ,  $(2kl)$ ,  $(hko)$ , and  $(h0l)$  using Ni-filtered  $\text{CuK}\alpha$  radiation. A total of 934 independent  $hkl$  reflections with  $I > 2\sigma(I)$  were measured with a diffractometer of the Arndt Phillips design using  $\text{MoK}\alpha$  radiation monochromated by reflection from a graphite crystal and using a scintillation counter in conjunction with a pulse height analyser. Lorentz polarization corrections were applied and absorption correction was made using Well's method.<sup>1</sup>

### STRUCTURE DETERMINATION

The symmetry of the Weissenberg and precession photographs is in agreement with the space group  $Pnma$  (No. 62). A three-dimensional Patterson function gave the positions (0.22, 0.01, 0.12), and (0.40, 0.15, 0.37) for two hol-

mium atoms. A three-dimensional Fourier map phased on this assumption gave the position (0.42, 0.14, 0.87) of the germanium atom. A new Fourier map based on structure factor signs calculated with all the heavy atoms gave the positions of all the oxygen atoms and the sodium atom. The refinement proceeded by the methods of least squares (G 403),<sup>2</sup> using isotropic temperature factors, giving an  $R$ -value of 8.5 %. A final difference Fourier map showed no extra atoms.

Table 1. Atomic coordinates and temperature factors with standard deviations. Diffractometer data, 934 reflections,  $R = 8.5$  %.

Atom	$x$	$y$	$z$	$B$ (Å <sup>2</sup> )
O <sub>1</sub>	0.221 (3)	0.1163 (9)	0.075 (3)	0.3 (3)
O <sub>2</sub>	0.390 (3)	0.0438 (9)	0.384 (3)	0.3 (3)
O <sub>3</sub>	0.48 (1)	0.25 (0)	0.342 (9)	6.3 (1.5)
O <sub>4</sub>	0.087 (3)	0.1589 (9)	0.427 (3)	0.5 (3)
O <sub>5</sub>	0.390 (4)	0.173 (1)	0.709 (3)	1.1 (4)
O <sub>6</sub>	0.454 (3)	0.0466 (9)	0.859 (3)	0.6 (3)
Na	0.150 (2)	0.25 (0)	0.694 (2)	0.0 (2)
Ge	0.4214 (5)	0.1258 (2)	0.9103 (4)	0.60 (5)
Ho <sub>1</sub>	0.2201 (2)	0.01227 (6)	0.1258 (2)	0.43 (2)
Ho <sub>2</sub>	0.4080 (2)	0.15002 (7)	0.3774 (2)	0.55 (2)

Table 2. Interatomic distances in Å and bond angles in degrees. Standard deviations in parentheses.

Ge—O <sub>1</sub>	1.780 (20)	O <sub>1</sub> —Ge—O <sub>5</sub>	119.3 (9)
Ge—O <sub>5</sub>	1.741 (23)	O <sub>1</sub> —Ge—O <sub>4</sub> '	96.9 (8)
Ge—O <sub>4</sub> '	1.744 (21)	O <sub>1</sub> —Ge—O <sub>6</sub>	96.3 (8)
Ge—O <sub>6</sub>	1.766 (21)	O <sub>5</sub> —Ge—O <sub>4</sub> '	110.6 (9)
		O <sub>5</sub> —Ge—O <sub>6</sub>	115.2 (9)
Ho <sub>1</sub> —O <sub>2</sub> '	2.333 (20)	O <sub>4</sub> '—Ge—O <sub>6</sub>	116.8 (8)
Ho <sub>1</sub> —O <sub>2</sub> ''	2.194 (19)		
Ho <sub>1</sub> —O <sub>6</sub> ''	2.366 (20)	O <sub>1</sub> —Ho <sub>1</sub> —O <sub>4</sub> '	73.1 (8)
Ho <sub>1</sub> —O <sub>1</sub>	2.281 (21)	O <sub>1</sub> —Ho <sub>1</sub> —O <sub>5</sub> ''	119.8 (8)
Ho <sub>1</sub> —O <sub>2</sub>	2.229 (19)	O <sub>2</sub> '—Ho <sub>1</sub> —O <sub>6</sub> ''	167.0 (8)
Ho <sub>1</sub> —O <sub>6</sub>	2.537 (20)	O <sub>6</sub> '—Ho <sub>1</sub> —O <sub>2</sub> ''	93.0 (8)
Ho <sub>1</sub> —O <sub>6</sub> ''	2.547 (22)	O <sub>2</sub> —Ho <sub>1</sub> —O <sub>6</sub>	100.0 (8)
Ho <sub>2</sub> —O <sub>1</sub>	2.545 (19)		
		O <sub>1</sub> —Ho <sub>2</sub> —O <sub>4</sub> '	64.0 (8)
Ho <sub>2</sub> —O <sub>4</sub>	2.199 (22)	O <sub>1</sub> —Ho <sub>2</sub> —O <sub>5</sub>	146.8 (8)
Ho <sub>2</sub> —O <sub>2</sub>	2.305 (20)	O <sub>4</sub> '—Ho <sub>2</sub> —O <sub>5</sub>	148.3 (8)
Ho <sub>2</sub> —O <sub>4</sub> '	2.432 (20)	O <sub>2</sub> —Ho <sub>2</sub> —O <sub>4</sub>	91.8 (8)
Ho <sub>2</sub> —O <sub>5</sub>	2.236 (18)	O <sub>1</sub> '—Ho <sub>2</sub> —O <sub>6</sub>	97.0 (9)
Ho <sub>2</sub> —O <sub>1</sub> '	2.262 (20)		
Ho <sub>2</sub> —O <sub>5</sub>	2.347 (22)		
Na'—O <sub>3</sub>	3.402 (50)		
Na'—O <sub>5</sub>	2.510 (27)		
Na'—O <sub>4</sub> '	2.738 (23)		
Na'—O <sub>6</sub> '	2.330 (27)		
Na'—O <sub>3</sub> '	2.459 (50)		

Table 3. Observed and calculated structure factors.

h	k	l	Fo	Fc	0 3 9	1 0 5	2 10 1	2 3 6		
0 4 0	121	-166			1 0 5	127	-120	2 3 6	75	-62
0 6 0	657	821			1 3 5	55	39	2 4 6	62	57
0 8 0	604	701			1 5 5	171	163	2 5 6	70	66
0 10 0	278	-264			1 6 5	166	-153	2 7 6	61	66
0 12 0	188	178			1 9 5	90	83	2 8 6	66	-60
0 14 0	302	350			1 10 5	164	158	2 9 6	62	-87
0 20 0	185	198			1 11 5	287	278	2 11 6	57	-45
0 22 0	105	-115			1 12 5	162	-159	2 13 6	70	62
0 24 0	68	-101			1 13 5	181	177	2 15 6	48	39
0 28 0	121	-130			1 14 5	142	-136	2 16 6	52	-32
0 3 1	155	-139			1 16 5	189	192	2 17 6	83	-67
0 5 1	152	134			1 17 5	244	251	2 20 7	66	-52
0 7 1	298	-300			1 18 5	53	51	2 2 7	100	94
0 9 1	332	-363			1 19 5	281	274	2 4 7	151	142
0 13 1	154	-172			1 20 5	228	-232	2 5 7	117	-108
0 15 1	460	-538			1 21 5	65	58	2 6 7	97	-93
0 17 1	74	-72			1 22 5	95	90	2 8 7	80	79
0 21 1	330	-390			1 23 5	63	76	2 9 7	73	-70
0 23 1	241	-261			1 24 5	159	162	2 10 7	211	203
0 25 1	65	70			1 25 5	213	233	2 11 7	203	-190
0 27 1	136	-180			1 0 6	88	73	2 12 7	61	-48
0 29 1	208	-241			1 1 6	266	232	2 13 7	127	-117
0 0 2	73	79			1 2 6	350	336	2 14 7	101	-90
0 2 2	56	40			1 3 6	132	134	2 16 7	198	193
0 4 2	183	-175			1 4 6	436	395	2 17 7	184	-173
0 6 2	35	24			1 5 6	240	-228	2 19 7	211	-188
0 8 2	88	97			1 6 6	132	137	2 20 7	194	-166
0 12 2	125	-113			1 7 6	120	131	2 0 8	117	-116
0 14 2	58	43			1 8 6	174	161	2 1 8	167	166
0 20 2	57	-46			1 9 6	254	233	2 2 8	245	-226
0 28 2	48	-50			1 10 6	365	352	2 3 8	53	37
0 1 3	287	-246			1 11 6	139	-124	2 4 8	277	-257
0 3 3	64	-55			1 12 6	133	122	2 5 8	221	-194
0 5 3	104	-100			1 13 6	44	-47	2 6 8	139	-130
0 7 3	352	-358			1 15 6	205	209	2 8 8	148	-141
0 9 3	328	-300			1 16 6	157	153	2 9 8	115	117
0 11 3	154	150			1 18 6	84	76	2 10 8	239	-224
0 13 3	267	-265			1 19 6	89	80	2 11 8	234	-225
0 15 3	454	-478			1 20 6	93	-104	2 12 8	111	-98
0 21 3	357	-418			1 21 6	143	144	2 13 8	115	-103
0 23 3	207	-237			1 0 7	236	235	2 15 8	98	91
0 25 3	55	74			1 1 7	81	69	2 16 8	130	-112
0 27 3	108	-135			1 4 7	145	-137	2 0 9	142	116
0 0 4	932	-926			1 5 7	178	-183	2 1 9	63	-53
0 2 4	324	-312			1 6 7	147	136	2 2 9	102	-84
0 4 4	38	33			1 7 7	120	-109	2 3 9	237	-218
0 6 4	612	-593			1 8 7	136	146	2 4 9	76	60
0 8 4	467	-468			1 10 7	119	-110	2 5 9	65	-71
0 10 4	141	136			1 11 7	159	-137	2 6 9	134	-117
0 12 4	150	-144			1 13 7	206	-201	2 7 9	177	-176
0 14 4	365	-360			1 14 7	126	118	2 8 9	199	304
0 16 4	57	62			1 15 7	114	-97	2 9 9	125	-122
0 20 4	186	-209			1 17 7	141	-147	2 10 9	266	267
0 22 4	60	75			1 19 7	194	-167	2 11 9	47	-53
0 24 4	132	156			1 0 8	66	-53	2 12 9	134	-137
0 1 5	210	203			1 1 8	59	65	2 13 9	180	201
0 3 5	129	125			1 3 8	62	56	2 14 9	76	44
0 5 5	148	-142			1 4 8	46	-41	2 15 9	350	441
0 7 5	171	149			1 5 8	88	-71	2 16 9	142	-29
0 9 5	324	315			1 6 8	95	-63	2 17 9	45	-41
0 13 5	106	93			1 7 8	80	-90	2 18 9	323	367
0 15 5	346	332			1 8 8	51	-46	2 19 9	197	210
0 17 5	168	169			1 9 8	70	72	2 20 9	46	31
0 19 5	68	66			1 13 8	62	-61	2 21 9	68	-66
0 21 5	231	238			1 0 9	146	152	2 22 9	99	124
0 23 5	175	185			1 1 9	52	56	2 23 9	1005	972
0 0 6	165	-166			1 2 9	199	199	2 1 10	74	65
0 2 6	193	198			1 3 9	156	-162	2 2 10	268	256
0 4 6	45	-41			1 4 9	110	108	2 3 10	59	57
0 6 6	123	-123			1 5 9	219	223	2 4 10	177	-166
0 8 6	110	111			1 6 9	263	277	2 5 10	43	29
0 10 6	61	-61			1 7 9	125	-136	2 6 10	618	579
0 12 6	87	72			1 8 9	93	96	2 7 10	98	96
0 1 7	147	139			1 23 9	136	146	2 8 10	501	491
0 3 7	44	48			1 24 9	91	121	2 9 10	183	169
0 5 7	53	-52			1 25 9	177	213	2 10 10	283	-176
0 7 7	224	203			1 26 9	63	-84	2 11 10	99	90
0 9 7	229	223			1 27 9	115	115	2 12 10	89	85
0 11 7	91	-78			1 0 10	102	106	2 13 10	142	142
0 13 7	151	136			1 1 10	72	-72	2 14 10	344	346
0 15 7	334	322			1 2 10	38	-36	2 15 10	190	186
0 17 7	63	41			1 3 10	94	-101	2 16 10	138	134
0 0 8	453	419			1 4 10	118	119	2 17 10	83	94
0 2 8	203	200			1 5 10	45	34	2 18 10	148	177
0 4 8	84	77			1 6 10	65	-55	2 19 10	225	178
0 6 8	383	377			1 7 10	43	-51	2 20 10	65	-54
0 8 8	227	199			1 11 10	83	-84	2 21 10	118	120
0 10 8	66	-53			1 13 10	82	81	2 22 10	106	-123
0 12 8	182	170			1 15 10	47	46	2 23 10	70	105
0 14 8	257	256			1 17 10	57	-55	2 0 11	202	184
0 16 8	102	-111			1 19 10	46	-56	2 1 11	235	-214
0 1 9	175	-161			1 21 10	68	67	2 2 11	185	171
								2 3 11	95	-89
								2 4 11	91	77

Table 3. Continued.

3 5 3 152 137	4 16 0 153 178	4 9 6 65 -64	5 4 6 205 201	6 6 5 180 176
3 6 3 196 185	4 17 0 180 198	4 11 6 70 -64	5 5 6 338 302	6 7 5 70 -59
3 7 3 214 -131	4 18 0 104 97	4 13 6 93 73	5 6 6 76 73	6 8 5 119 109
3 8 3 74 70	4 19 0 87 78	4 0 7 173 -186	5 8 6 101 91	6 9 5 187 -167
3 9 3 307 -289	4 20 0 118 -131	4 1 7 69 -81	5 9 6 76 -70	6 10 5 58 36
3 10 3 62 56	4 21 0 196 226	4 2 7 64 -65	5 10 6 157 137	6 11 5 63 32
3 11 3 66 45	4 23 0 123 144	4 4 7 69 -66	5 11 6 311 288	6 12 5 109 96
3 12 3 58 48	4 3 1 44 29	4 5 7 96 119	5 12 6 92 94	6 14 5 97 89
3 13 3 140 125	4 4 1 78 85	4 6 7 184 -186	5 13 6 228 207	6 15 5 167 -154
3 14 3 92 82	4 5 1 205 -194	4 8 7 60 -68	5 0 7 75 -62	6 0 6 129 121
3 15 3 345 -341	4 6 1 294 286	4 11 7 201 190	5 2 7 171 158	6 4 6 103 -104
3 17 3 104 -100	4 8 1 114 124	4 12 7 153 -146	5 4 7 302 277	6 8 6 111 87
3 21 3 244 -268	4 11 1 224 -242	4 13 7 101 96	5 5 7 125 -97	6 0 7 209 189
3 23 3 157 -176	4 12 1 170 185	4 14 7 114 -119	5 7 7 78 -88	6 1 7 99 -77
3 24 3 50 -41	4 13 1 180 -195	4 16 7 102 97	5 10 7 200 211	6 2 7 113 119
3 0 4 199 196	4 14 1 177 195	4 2 8 146 169	5 11 7 89 -63	6 6 7 158 149
3 3 4 35 26	4 16 1 121 -126	4 4 8 222 250	5 12 7 88 85	7 3 1 29 -29
3 4 4 179 -170	4 17 1 193 -220	4 7 8 140 149	5 1 8 66 -45	7 4 1 136 -157
3 6 4 53 39	4 19 1 214 -252	4 9 8 221 187	6 4 0 189 257	7 5 1 126 126
3 7 4 39 27	4 20 1 136 159	4 10 8 222 213	6 6 0 318 -361	7 6 1 208 -218
3 8 4 115 117	4 21 1 57 -28	4 0 9 221 230	6 7 0 156 -180	7 7 1 57 -70
3 9 4 37 -20	4 22 1 54 -53	5 3 1 85 -85	6 8 0 232 -265	7 8 1 94 -109
3 10 4 43 -39	4 23 1 58 -56	5 4 1 234 222	6 9 0 167 -198	7 9 1 73 -70
3 12 4 76 -74	4 24 1 152 -166	5 5 1 84 -76	6 10 0 163 175	7 10 1 45 -34
3 16 4 65 69	4 25 1 200 -214	5 8 1 179 192	6 11 0 115 -122	7 11 1 150 160
3 20 4 70 -63	4 2 2 39 -24	5 9 1 103 -103	6 13 0 147 -183	7 12 1 170 -188
3 0 5 192 191	4 3 2 65 63	5 10 1 312 322	6 14 0 247 -235	7 13 1 58 59
3 1 5 124 -106	4 4 2 43 28	5 11 1 181 -184	6 15 0 247 -276	7 14 1 105 -132
3 2 5 109 94	4 5 2 53 -55	5 14 1 54 -64	6 16 0 68 71	7 15 1 91 -89
3 3 5 60 -50	4 6 2 37 -14	5 16 1 220 256	6 17 0 135 -153	7 16 1 74 71
3 4 5 88 85	4 7 2 54 -55	5 17 1 134 -150	6 19 0 128 -156	7 17 1 93 110
3 5 5 73 65	4 11 2 62 62	5 18 1 59 80	6 20 0 86 -108	7 0 2 166 -159
3 6 5 110 95	4 12 2 49 34	5 19 1 128 -156	6 21 0 209 -232	7 1 2 198 194
3 7 5 254 -232	4 13 2 53 -59	5 20 1 191 -213	6 4 1 126 -129	7 2 2 127 120
3 8 5 128 129	4 0 3 227 207	5 1 2 279 263	6 5 1 89 -89	7 3 2 183 184
3 9 5 221 -199	4 1 3 120 106	5 2 2 228 -218	6 6 1 167 -182	7 4 2 243 235
3 11 5 110 99	4 2 3 101 99	5 3 2 114 108	6 7 1 118 126	7 5 2 141 -123
3 12 5 55 54	4 4 3 137 141	5 4 2 300 -286	6 8 1 173 -182	7 6 2 101 -97
3 13 5 141 -129	4 5 3 175 -163	5 5 2 433 -410	6 9 1 158 169	7 7 2 115 104
3 14 5 71 48	4 6 3 265 246	5 6 2 107 -105	6 11 1 127 -123	7 8 2 45 -35
3 15 5 396 -373	4 7 3 58 51	5 7 2 93 -86	6 12 1 77 -78	7 9 2 315 310
3 16 5 46 30	4 8 3 74 66	5 8 2 71 -53	6 13 1 59 61	7 10 2 239 230
3 19 5 59 56	4 10 3 55 -55	5 9 2 142 139	6 14 1 95 -101	7 11 2 131 135
3 21 5 313 -309	4 11 3 303 -297	5 10 2 238 -228	6 15 1 209 243	7 13 2 69 70
3 23 5 190 -190	4 12 3 232 230	5 11 2 317 -316	6 19 1 82 -87	7 14 2 113 -108
3 0 6 601 -550	4 13 3 118 -111	5 12 2 121 -126	6 20 1 65 -65	7 15 2 242 235
3 2 6 172 -157	4 14 3 148 151	5 13 2 336 -337	6 21 1 191 212	7 16 2 114 131
3 3 6 58 -56	4 16 3 143 -145	5 16 2 55 -57	6 0 2 84 -79	7 0 3 267 257
3 6 6 444 -403	4 17 3 204 -210	5 17 2 187 -207	6 4 2 56 54	7 1 3 112 101
3 7 6 105 -109	4 19 3 239 -255	5 18 2 63 -63	6 7 2 38 18	7 2 3 115 118
3 8 6 277 -256	4 20 3 167 197	5 19 2 292 -340	6 8 2 74 -68	7 3 3 62 44
3 9 6 122 -102	4 22 3 62 -58	5 21 2 79 -71	6 16 2 58 -35	7 4 3 109 101
3 10 6 119 112	4 24 3 155 -177	5 23 2 118 -122	6 0 3 288 -288	7 5 3 136 -125
3 11 6 86 -74	4 1 4 276 -253	5 0 3 45 35	6 1 3 102 93	7 6 3 229 213
3 12 6 182 -162	4 2 4 280 -264	5 2 3 239 -223	6 2 3 168 -167	7 7 3 54 45
3 13 6 112 -92	4 3 4 199 -193	5 4 3 328 -308	6 3 3 39 17	7 8 3 161 161
3 14 6 273 -246	4 4 4 427 -398	5 5 3 125 119	6 4 3 75 -76	7 9 3 77 67
3 15 6 169 -160	4 5 4 178 166	5 8 3 111 -105	6 5 3 112 -95	7 11 3 129 -120
3 16 6 83 84	4 7 4 139 -129	5 9 3 75 68	6 6 3 206 -200	7 12 3 166 144
3 17 6 110 -87	4 8 4 99 -91	5 10 3 312 -297	6 7 3 201 187	7 13 3 80 -70
3 19 6 94 -94	4 9 4 369 -351	5 11 3 114 107	6 8 3 163 -158	7 14 3 131 130
3 20 6 178 -182	4 10 4 347 -339	5 13 3 96 105	6 9 3 121 114	7 15 3 82 55
3 21 6 143 -114	4 12 4 115 -106	5 14 3 65 44	6 10 3 51 -50	7 0 4 59 -51
3 0 7 126 -121	4 14 4 53 53	5 16 3 178 -181	6 11 3 154 -146	7 1 4 58 66
3 1 7 159 145	4 15 4 278 -276	5 17 3 111 109	6 12 3 62 -64	7 3 4 55 42
3 2 7 109 -90	4 16 4 167 -175	5 18 3 64 -55	6 13 3 96 81	7 5 4 58 -43
3 3 7 114 114	4 17 4 141 -132	5 19 3 104 107	6 14 3 99 -90	7 7 4 76 -76
3 4 7 98 -99	4 18 4 94 -81	5 20 3 119 138	6 15 3 274 270	7 9 4 68 60
3 5 7 124 -117	4 19 4 65 -48	5 1 4 58 57	6 16 3 56 -23	7 0 5 155 153
3 6 7 108 -90	4 20 4 119 125	5 3 4 41 44	6 17 3 72 -68	7 1 5 89 81
3 7 7 80 65	4 21 4 209 -224	5 4 4 74 -72	6 19 3 80 -87	7 2 5 130 124
3 8 7 71 -73	4 23 4 121 -153	5 5 4 46 -47	6 0 4 446 421	7 4 5 130 114
3 9 7 259 238	4 0 5 312 -298	5 8 4 45 38	6 1 4 76 72	7 5 5 107 -95
3 11 7 50 -47	4 1 5 110 -100	5 9 4 63 54	6 2 4 48 43	7 6 5 216 202
3 12 7 57 -64	4 2 5 88 -80	5 12 4 54 -47	6 3 4 71 71	7 9 5 85 70
3 14 7 75 -50	4 3 5 59 -36	5 13 4 49 -41	6 4 4 167 -144	7 0 6 133 110
3 15 7 241 217	4 4 5 48 14	5 15 4 51 -27	6 6 4 304 275	7 1 6 148 -130
3 17 7 153 137	4 5 5 181 173	5 0 5 56 -56	6 7 4 137 135	8 4 0 55 96
3 0 8 118 -103	4 6 5 264 -241	5 2 5 188 -176	6 8 4 219 212	8 5 0 261 320
3 4 8 127 118	4 8 5 181 -176	5 3 5 83 82	6 9 4 215 195	8 11 0 260 294
3 8 8 103 -90	4 10 5 57 31	5 4 5 198 -177	6 10 4 165 -156	8 3 1 33 -36
3 0 9 116 -102	4 11 5 175 162	5 5 5 59 36	6 11 4 91 100	8 4 1 234 233
3 1 9 113 107	4 12 5 116 -102	5 8 5 144 -138	6 12 4 59 58	8 8 1 112 133
3 6 9 102 -83	4 13 5 170 159	5 9 5 80 62	6 13 4 149 154	8 10 1 233 244
3 7 9 156 130	4 14 5 154 -157	5 10 5 276 -270	6 14 4 218 201	8 0 3 57 59
4 4 0 403 492	4 16 5 60 34	5 11 5 170 169	6 15 4 257 247	8 1 3 51 -38
4 5 0 188 -217	4 17 5 155 144	5 14 5 90 67	6 16 4 66 -76	8 2 3 197 188
4 6 0 48 6	4 19 5 179 174	5 16 5 224 -222	6 17 4 169 153	8 4 3 190 173
4 7 0 93 95	4 20 5 85 -71	5 17 5 135 114	6 0 5 218 211	8 8 3 138 142
4 8 0 76 105	4 1 6 65 -71	5 19 5 159 145	6 1 5 148 -132	8 0 4 185 155
4 9 0 409 472	4 3 6 78 -77	5 0 6 80 78	6 2 5 158 150	
4 10 0 393 442	4 4 6 48 -42	5 1 6 214 -195	6 3 5 71 -75	
4 12 0 68 86	4 5 6 95 90	5 2 6 156 135	6 4 5 125 128	
4 15 0 221 249	4 7 6 78 75	5 3 6 67 -47	6 5 5 131 119	

## CRYSTAL DATA

The formula of the compound is  $\text{NaHo}_4(\text{GeO}_4)_2\text{O}_2\text{OH}$ , and the unit cell contains four formula units. The crystal system is orthorhombic, and the space group is  $Pnma$  (No. 62). The axes are  $a = 6.75 \text{ \AA}$ ,  $b = 21.67 \text{ \AA}$ ,  $c = 6.91 \text{ \AA}$ . The calculated density is  $6.60 \text{ g/cm}^3$  and the absorption coefficient for Mo-radiation is  $274 \text{ cm}^{-1}$ . The structure factors for the oxygen and for the sodium atoms were calculated using atomic scattering factors from Vol. III of *International Tables of X-Ray Crystallography*. The structure factors for the holmium atoms were calculated from the atomic scattering factors reported by Cromer and Mann.<sup>3</sup> The atomic scattering factors were approximated by Bassi<sup>4</sup> polynomials. Atomic coordinates and temperature factors are listed in Table 1, and interatomic distances and bond angles in Table 2. Observed and calculated structure factors are listed in Table 3. Fig. 1 is a projection of the  $\text{HoO}_7$  coordination polyhedra on the plane (001), and Fig. 2 shows the coordination of the germanium and the sodium atoms with the oxygen atoms in projection on the same plane.

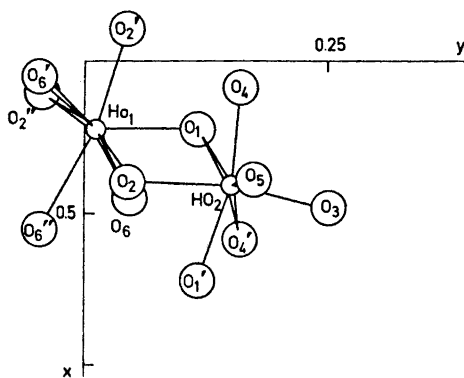


Fig. 1. Projection of the  $\text{HoO}_7$  coordination polyhedra on (001).

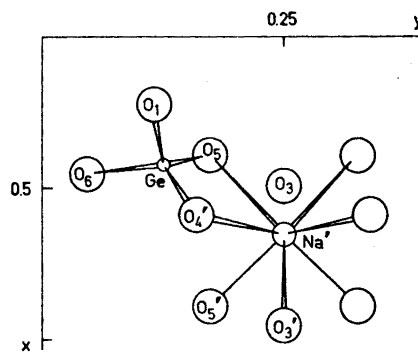


Fig. 2. Projection of the  $\text{GeO}_4$  coordination polyhedron and the sodium-oxygen coordination polyhedron on (001).

## DISCUSSION

The crystal structure of  $\text{NaHo}_4(\text{GeO}_4)_2\text{O}_2\text{OH}$  comprises  $\text{HoO}_7$  polyhedra and  $\text{GeO}_4$  tetrahedra. The  $\text{GeO}_4$  tetrahedra are fairly regular and the distances from Ge to  $\text{O}_1$ ,  $\text{O}_6$ ,  $\text{O}_4'$ , and  $\text{O}_5$  have a mean of  $1.758 \text{ \AA}$ ,  $\sigma = 0.011 \text{ \AA}$ . The distances from Ge to  $\text{O}_1$  and  $\text{O}_6$  have a mean value of  $1.773 \text{ \AA}$ ,  $\sigma = 0.015 \text{ \AA}$ , and the distances from Ge to  $\text{O}_4'$  and  $\text{O}_5$  have a mean value of  $1.743 \text{ \AA}$ ,  $\sigma = 0.016 \text{ \AA}$ . These distances are comparable with the Ge-O distances found in the quartz modification of  $\text{GeO}_2$ ,<sup>5</sup> and in  $\text{Na}_4\text{Ge}_9\text{O}_{20}$ ,<sup>6</sup>  $\text{Na}_8\text{Sn}_4\text{Ge}_{10}\text{O}_{30}(\text{OH})_4$ ,<sup>7</sup> and  $\text{Na}_4\text{Sn}_2\text{Ge}_4\text{O}_{12}(\text{OH})_4$ .<sup>8</sup> The oxygen atoms of the  $\text{GeO}_4$  tetrahedra are coordinated to the following atoms:  $\text{O}_1$  to Ge,  $\text{Ho}_1$ ,  $\text{Ho}_2$ , and  $\text{Ho}_1'$ ;  $\text{O}_6$  to Ge,  $\text{Ho}_1$ ,  $\text{Ho}_1'$ , and  $\text{Ho}_1''$ ;  $\text{O}_4'$  to Ge,  $\text{Ho}_2$ ,  $\text{Ho}_2'$ , and  $\text{Na}'$ ; and  $\text{O}_5$  to Ge,  $\text{Ho}_2$ ,  $\text{Na}$ , and  $\text{Na}'$ . The  $\text{GeO}_4$  tetrahedron is thus only linked to the holmium and the sodium coordination polyhedra.

The two holmium atoms are each coordinated with seven oxygen atoms (see Fig. 1).  $\text{Ho}_1$  is coordinated with  $\text{O}_6, \text{O}_6',$  and  $\text{O}_6''$ , which are also coordinated with the germanium atoms, and with  $\text{O}_2, \text{O}_2',$  and  $\text{O}_2''$ . The oxygen atom  $\text{O}_2$  is coordinated tetrahedrally with four holmium atoms,  $\text{Ho}_1, \text{Ho}_1', \text{Ho}_1'',$  and  $\text{Ho}_2$ . The holmium atom  $\text{Ho}_2$  is coordinated with  $\text{O}_1, \text{O}_1', \text{O}_4, \text{O}_4',$  and  $\text{O}_5$  which all are coordinated with germanium atoms, with  $\text{O}_2$  which is coordinated with holmium atoms only, and with  $\text{O}_3$  which is coordinated with one sodium atom.  $\text{O}_3$  is assumed to be the oxygen atom in the  $\text{OH}^-$  ion. The  $\text{HoO}_7$  coordination polyhedra are of the same type as the polyhedra found in the monoclinic modification of holmium oxide hydroxide.<sup>9</sup> The polyhedron around  $\text{Ho}_2$  is fairly regular. Six oxygen atoms form a trigonal prism, and the seventh atom,  $\text{O}_5$ , lies along a normal to a prism face (Fig. 1). The polyhedron around  $\text{Ho}_1$  is distorted in comparison with the polyhedron of  $\text{Ho}_2$  and the polyhedra found in monoclinic holmium oxide hydroxide. Six oxygen atoms form a trigonal prism (Fig. 1) with the seventh atom,  $\text{O}_6''$ , displaced so that the angle  $\text{O}_6''-\text{Ho}_1-\text{O}_2'$  of  $167.0^\circ$  is much greater than the angle  $\text{O}_1-\text{Ho}_2-\text{O}_5$  of  $146.8^\circ$ . The coordination polyhedron around  $\text{Ho}_1$  could be described as a distorted cube with one corner omitted.

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